



**ODA E INXHINIERËVE  
TË REPUBLIKËS SË KOSOVËS**

# **Piketimi dhe kontrolli gjeodezik i ndërtimit dhe monitorimi i deformimeve dhe stabilitetit të objekteve**

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## Training objectives

- ✓ Understand geodetic stakeout and construction control procedures
- ✓ Explain accuracy requirements and design principles for engineering geodetic networks
- ✓ Present methodologies for deformation analysis and stability assessment
- ✓ Introduce monitoring systems for engineering structures and infrastructure
- ✓ Compare classical and modern monitoring approaches including GNSS, total stations and InSAR
- ✓ Demonstrate practical applications through real engineering case studies
- ✓ Support reliable engineering decision-making through accurate geodetic monitoring

*“Reliable geodetic monitoring is essential for safe, accurate and sustainable infrastructure.”*

# Agenda – Contents

## **A Priori Accuracy and Network Design**

- A priori accuracy analysis
- Engineering geodetic network design
- Observation planning and optimization

## **Construction Stakeout, Control and Quality Assessment**

- Horizontal and vertical stakeout methods
- Error ellipses and tolerance assessment
- Accuracy verification and quality control

## **Deformation Analysis and Monitoring**

- Mathematical models for deformation analysis
- Classical and modern monitoring approaches
- Monitoring systems for engineering structures

## **Practical Applications**

- Engineering structures and infrastructure
- Dams and deformation monitoring
- Selected real engineering case studies

*“From mathematical network design to engineering monitoring and decision support.”*

## A priori accuracy for engineering geodetic networks

- ❑ A priori analysis of a geodetic network is the mathematical process of isolating and evaluating network quality *before any field observations are made*. It relies on a critical principle of Least Squares estimation: **the precision of adjusted coordinates depends entirely on network geometry and observation weights, not on the actual field measurement values.**
- ❑ In structural engineering and construction stakeout, we must prove mathematically that our planned network can isolate true structural deformation or position structural elements within design tolerances. If the pre-analysis reveals that our measurement layout cannot meet these thresholds, the network configuration must be redesigned.
- ❑ Contents:
  1. Identify Structure Class
  2. Define Instrument Error Budgets
  3. Build the Stochastic Model
  4. Optimize Station Geometry

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## 1. Identify Structure Class

Classify the project to find its tolerance tier.

- Tier 1: High-precision manufacturing and industrial machinery.
- Tier 2: Bridges, high-rise buildings, and tunnels.
- Tier 3: General earthworks, roads, and utilities.

## 2. Define Instrument Error Budgets

Quantify the sensory limits of field hardware.

- Total station angular limits ( $\sigma_{\alpha} = \pm 0.5''$  to  $\pm 5''$ ).
- Total station distance limits ( $\sigma_d = \pm 1 \text{ mm} \pm 1 \text{ ppm}$ ).
- GNSS RTK vector limits ( $\sigma_{RTK} = \pm 8 \text{ mm} \pm 1 \text{ ppm}$ ).
- Digital leveling limits ( $\sigma_z = \pm 0.3 \text{ mm/km}$ ).

### 3. Build the Stochastic Model

Compute the theoretical error propagation matrix.

The geometric strength of the network is simulated using the design matrix **A** and the observation weight matrix **P** to output the a priori variance-covariance matrix **C<sub>x</sub>**:

$$\mathbf{C}_x = \sigma_0^2 (\mathbf{A}^T \mathbf{P} \mathbf{A})^{-1}$$

Where:

- $\sigma_0^2$  is the a priori reference variance.
- **A** contains partial derivatives of the network geometry configuration.
- **P** is the weight matrix derived from instrument error budgets.

### 4. Optimize Station Geometry

Adjust network layout until ellipses fall within limits.

- Extract point coordinate standard deviations ( $\sigma_x, \sigma_y, \sigma_z$ ).
- Calculate the dimensions of the error ellipses.
- Add stations or lines of sight if ellipses exceed structural limits. ?

## General Construction Accuracy Requirements Matrix

Construction Project Type	Relative Precision Range	Absolute Positional Accuracy ( $\sigma_{x,y}$ )	Vertical Accuracy ( $\sigma_z$ )	Typical Instrument Mix
Industrial / Particle Accelerators	> 1 : 500,000	$\pm 0.5$ mm to $\pm 1.5$ mm	$\pm 0.2$ mm	Laser Trackers, Sub-second Total Stations
High-Rise Buildings & Tunnels	1 : 100,000 – 1 : 200,000	$\pm 2$ mm to $\pm 5$ mm	$\pm 1$ mm to $\pm 2$ mm	1" Total Stations, Precise Digital Levels
Standard Commercial Buildings	1 : 20,000 – 1 : 50,000	$\pm 5$ mm to $\pm 10$ mm	$\pm 5$ mm	3" Total Stations, GNSS Network RTK
Earthworks, Roads, & Utilities	1 : 10,000 – 1 : 20,000	$\pm 15$ mm to $\pm 25$ mm	$\pm 20$ mm	GNSS RTK, Machine Control Sensors

## The Three Orders of Network Design

Geodetic optimization is categorized into distinct design phases:

- **Zero-Order Design (ZOD):** Solving for the optimal reference system (datum definition).
- **First-Order Design (FOD):** Solving for the optimal geometric configuration (where to place stations and targets).
- **Second-Order Design (SOD):** Solving for the optimal distribution of observation weights (choosing instruments and observation counts).

## Comprehensive Mathematical Framework

The entire mathematical base of a priori analysis is rooted in the Gauss-Markov model of Least Squares estimation:

- The Functional Model (The Design Matrix A)
- Distance Observation Equation
- Horizontal Direction Equation
- The Stochastic Model (The Weight Matrix P)
- The Fundamental Error Propagation

## The Functional Model (The Design Matrix **A**)

The functional model relates the unknown coordinates to the theoretical observations through non-linear geometric equations (distances, horizontal angles, azimuths, zenith angles). Let **x** be the vector of coordinate corrections, and **l** be the vector of observations. The linearized system is expressed as:

$$\mathbf{v} = \mathbf{Ax} - \mathbf{l}$$

Where **A** is the **Design Matrix** containing the partial derivatives of the observation equations with respect to the unknown parameters (coordinates).

### Distance Observation Equation

The spatial distance  $S_{ij}$  between station  $i(X_i, Y_i, Z_i)$  and target  $j(X_j, Y_j, Z_j)$  is:

$$S_{ij} = \sqrt{(X_j - X_i)^2 + (Y_j - Y_i)^2 + (Z_j - Z_i)^2}$$

The corresponding row in the **A** matrix consists of the partial derivatives relative to the variables of interest:

$$\frac{\partial S_{ij}}{\partial X_i} = -\frac{X_j - X_i}{S_{ij}}, \quad \frac{\partial S_{ij}}{\partial X_j} = \frac{X_j - X_i}{S_{ij}}$$

## Horizontal Direction Equation

The horizontal direction  $\alpha_{ij}$  from station  $i$  to target  $j$  utilizes the horizontal distance  $D_{ij} = \sqrt{(X_j - X_i)^2 + (Y_j - Y_i)^2}$ :

$$\alpha_{ij} = \arctan\left(\frac{Y_j - Y_i}{X_j - X_i}\right) - \omega_i$$

Where  $\omega_i$  is the unknown orientation uncorrected parameter of the total station instrument. The partial derivatives are:

$$\frac{\partial \alpha_{ij}}{\partial X_i} = \frac{Y_j - Y_i}{D_{ij}^2}, \quad \frac{\partial \alpha_{ij}}{\partial Y_i} = -\frac{X_j - X_i}{D_{ij}^2}, \quad \frac{\partial \alpha_{ij}}{\partial X_j} = -\frac{Y_j - Y_i}{D_{ij}^2}, \quad \frac{\partial \alpha_{ij}}{\partial Y_j} = \frac{X_j - X_i}{D_{ij}^2},$$

## The Stochastic Model (The Weight Matrix **P**)

The weight matrix **P** reflects the relative reliability and expected variances of different measurements. It is defined as the inverse of the a priori variance-covariance matrix of observations (**C<sub>l</sub>**):

$$\mathbf{P} = \sigma_0^2 \mathbf{C}_l^{-1}$$

Where  $\sigma_0^2$  is the a priori reference variance (typically set to 1). If observations are assumed to be statistically independent, **C<sub>l</sub>** is a diagonal matrix, and the weights are simply:

$$P_i = \frac{\sigma_0^2}{\sigma_i^2}$$

## The Fundamental Error Propagation

Applying the law of error propagation to the Least Squares normal equations yields the **A Priori Variance-Covariance Matrix of Parameters ( $\mathbf{C}_x$ )**:

$$\mathbf{C}_x = \sigma_0^2 (\mathbf{A}^T \mathbf{P} \mathbf{A})^{-1} = \sigma_0^2 \mathbf{N}^{-1}$$

Where  $\mathbf{N} = \mathbf{A}^T \mathbf{P} \mathbf{A}$  is the matrix of normal equations. Notice that  $\mathbf{C}_x$  **depends solely on the geometry ( $\mathbf{A}$ ) and instrument precisions ( $\mathbf{P}$ )**. No field measurements are required to evaluate it.

### 3. Rigorous Multi-Sensor Weight Matrix Formulation ( $\mathbf{P}$ )

When combining heterogeneous sensors—such as Terrestrial Total Stations (Angles/Distances) and GNSS (Baseline Vectors)—the observation variance-covariance matrix  $\mathbf{C}_l$  must be structured as a block-diagonal matrix to account for differing physical behaviors and stochastic correlations.

$$\mathbf{C}_l = \begin{bmatrix} \mathbf{C}_{\text{TotalStation}} & \mathbf{0} \\ \mathbf{0} & \mathbf{C}_{\text{GNSS}} \end{bmatrix}$$

## Total Station Sub-Matrix ( $C_{\text{TotalStation}}$ )

For an independent setup, this block is diagonal. The variances must account for instrument specifications, targeting errors, and centering errors.

$$\sigma_{\text{total}}^2 = \sigma_{\text{reading}}^2 + \sigma_{\text{centering}}^2 + \sigma_{\text{targeting}}^2$$

1. **Distance Measurements ( $S$ ):** Instrument specs are typically given as  $a$  mm +  $b$  ppm.

$$\sigma_S = \pm \sqrt{a^2 + (b \cdot 10^{-6} \cdot S)^2}$$

2. **Direction Measurements ( $\alpha$ ):** Angles degrade over short distances due to centering limits.

$$\sigma_{\alpha}^2 = \sigma_{\text{inst}}^2 + \frac{\sigma_{\text{center, inst}}^2 + \sigma_{\text{center, target}}^2}{D^2} \cdot \rho^2$$

Where  $\rho = 206264.8''/\text{radian}$ .

## GNSS Baseline Sub-Matrix ( $C_{\text{GNSS}}$ )

GNSS observations are entered into geodetic networks as 3D baseline vectors ( $\Delta X, \Delta Y, \Delta Z$ ) between points. These components are highly correlated due to atmospheric conditions and satellite geometry. For every baseline  $k$ , a fully populated  $3 \times 3$  covariance block must be inserted:

$$C_{\text{GNSS},k} = \begin{bmatrix} \sigma_X^2 & \sigma_{XY} & \sigma_{XZ} \\ \sigma_{YX} & \sigma_Y^2 & \sigma_{YZ} \\ \sigma_{ZX} & \sigma_{ZY} & \sigma_Z^2 \end{bmatrix}$$

These components are extracted directly from the GNSS baseline processing software engine based on carrier-phase ambiguities and carrier-to-noise ratios.

## Building the Global Weight Matrix

To calculate the overall weight matrix, invert each block independently and assemble them:

$$P = \sigma_0^2 \begin{bmatrix} C_{\text{TotalStation}}^{-1} & \mathbf{0} \\ \mathbf{0} & C_{\text{GNSS}}^{-1} \end{bmatrix}$$

# Mathematical Criteria for Network Quality Evaluation

## 1. Precision Criteria (Scalar Measures)

- **A-Optimality (Trace Criterion):** Minimizes the average variance of the coordinate parameters.

$$\text{Trace}(\mathbf{C}_x) = \sum_{i=1}^u \sigma_{x_i}^2 \rightarrow \text{Minimum}$$

- **D-Optimality (Determinant Criterion):** Minimizes the overall volume of the joint confidence ellipsoid.

$$\det(\mathbf{C}_x) \rightarrow \text{Minimum}$$

*For engineering stakeout, the semi-major axis  $(a)$  must be less than the design tolerance divided by the expansion factor chosen for your target confidence level (e.g., a 95% confidence level requires scaling the standard error ellipse by a factor of 2.45).*

## 2. Geometric Criteria (The Error Ellipse)

For any 2D point, the horizontal coordinate covariance sub-matrix is:

$$\mathbf{C}_{\text{point}} = \begin{bmatrix} \sigma_x^2 & \sigma_{xy} \\ \sigma_{yx} & \sigma_y^2 \end{bmatrix}$$

The dimensions and orientation of the **Standard Error Ellipse** are derived using eigenvalues and eigenvectors:

- **Semi-major axis ( $a$ ):**

$$a^2 = \frac{1}{2} \left( \sigma_x^2 + \sigma_y^2 + \sqrt{(\sigma_x^2 - \sigma_y^2)^2 + 4\sigma_{xy}^2} \right)$$

- **Semi-minor axis ( $b$ ):**

$$b^2 = \frac{1}{2} \left( \sigma_x^2 + \sigma_y^2 - \sqrt{(\sigma_x^2 - \sigma_y^2)^2 + 4\sigma_{xy}^2} \right)$$

- **Orientation Angle ( $\theta$  from North):**

$$\tan(2\theta) = \frac{2\sigma_{xy}}{\sigma_x^2 - \sigma_y^2}$$

### 3. Internal Reliability and Redundancy

A network can be precise but weak against undetected gross errors (blunders). **Internal reliability** measures the size of the marginally detectable blunder ( $\nabla_0 l_i$ ).

The **Redundancy Matrix (R)** is defined as:

$$\mathbf{R} = \mathbf{I} - \mathbf{A}(\mathbf{A}^T \mathbf{P} \mathbf{A})^{-1} \mathbf{A}^T \mathbf{P}$$

The diagonal elements  $r_i$  (redundancy numbers) range between  $0 \leq r_i \leq 1$ . They indicate how well an observation is checked by the surrounding network geometry.

- If  $r_i \rightarrow 0$ , the observation is uncontrolled. A blunder here cannot be detected and will directly warp the stakeout.
- If  $r_i \geq 0.35$ , the network geometry is considered robust enough to isolate systematic errors.

## Theoretical Breakdown of Accuracy Levels by Tier

*Civil and structural engineering tolerances govern the required geodetic network tier. Below is the theoretical breakdown of the mathematical limits for each level.*

### Tier 1: Sub-Millimeter Metrology Networks

- **Applications:** Particle accelerators, turbine alignments, high-speed rail tracks, aerospace manufacturing templates.
- **Mathematical Boundary:**  $\sigma_{x,y} \leq \pm 1.0$  mm,  $\sigma_z \leq \pm 0.5$  mm. Relative precision  $> 1 : 500,000$ .
- **Geometric Requirements:** Ultra-redundant braced configurations with inter-visible stations. Network configuration must avoid grazing sights near thermal surfaces to prevent refraction distortion.
- **Stochastic Profile:** Laser trackers or sub-second ( $\sigma_\alpha = 0.5''$ ) total stations. Forced-centering pillars are mandatory to eliminate human centering error ( $\sigma_{\text{center}} \rightarrow 0$ ).

### Tier 3: Standard Civil Infrastructure Networks

- **Applications:** Commercial developments, multi-story buildings, local highway pavements, bridge approach ramps.
- **Mathematical Boundary:**  $\sigma_{x,y} = \pm 5.0$  mm to  $\pm 10.0$  mm,  $\sigma_z = \pm 5.0$  mm. Relative precision  $1 : 20,000$  to  $1 : 50,000$ .
- **Geometric Requirements:** Open/closed traverses tied to regional public control networks (datums).
- **Stochastic Profile:** 3" total stations and real-time GNSS Network RTK or PPP configurations.

### Tier 2: Precision Engineering and Structural Networks

- **Applications:** High-rise structures, long-span suspension bridges, deep rail tunnels.
- **Mathematical Boundary:**  $\sigma_{x,y} = \pm 2.0$  mm to  $\pm 5.0$  mm,  $\sigma_z = \pm 1.0$  mm to  $\pm 2.0$  mm. Relative precision  $1 : 100,000$  to  $1 : 200,000$ .
- **Geometric Requirements:** Core control networks fixed with robust external reference datums. In tunnels, this requires zig-zag traverse structures with gyroscopic azimuth constraints to control lateral error drift.
- **Stochastic Profile:** 1" robotic total stations combined with static dual-frequency GNSS networks (minimum 1-hour sessions to resolve carrier phase ambiguities). Precise digital leveling loops with invar rods.

### Tier 4: Bulk Earthworks and Utility Networks

- **Applications:** Site grading, drainage lines, cut-and-fill calculations, preliminary corridor clearing.
- **Mathematical Boundary:**  $\sigma_{x,y} = \pm 15.0$  mm to  $\pm 25.0$  mm,  $\sigma_z = \pm 20.0$  mm to  $\pm 50$  mm. Relative precision  $1 : 5,000$  to  $1 : 10,000$ .
- **Geometric Requirements:** Sparse baselines optimized primarily for speed and area coverage.
- **Stochastic Profile:** Single-baseline GNSS RTK or machine automation sensors attached directly to excavators or graders.

# Observation Planning: How Many Measurements Are Enough?

## General Principle

Required network accuracy:

$$\sigma_{network} \leq \sigma_{required}$$

Observation precision improves with repeated measurements:

$$\sigma_{mean} = \frac{\sigma_{obs}}{\sqrt{n}}$$

where:

- $n$  = number of observation series
- $\sigma_{obs}$  = precision of a single observation

## General Observation Planning Model

Required number of observation series:

$$n \geq \left( \frac{\sigma_{instrument}}{\sigma_{required}} \right)^2$$

where:

$$\sigma_{instrument} = f(\text{distance, angle, centering, target, setup})$$

## Practical Conclusion

**The required number of measurements depends not only on instrument accuracy, but on the complete measurement system and required engineering tolerances.**

## Angular Observations (Total Station)

Required number of series:

$$n \geq \left( \frac{\sigma_{\alpha}}{\sigma_{required}} \right)^2$$

where:

- $\sigma_{\alpha}$  = angular precision of the instrument
- $\sigma_{required}$  = required angular precision

## Distance Observations (EDM)

EDM precision model:

$$\sigma_D = \sqrt{a^2 + b^2 D^2}$$

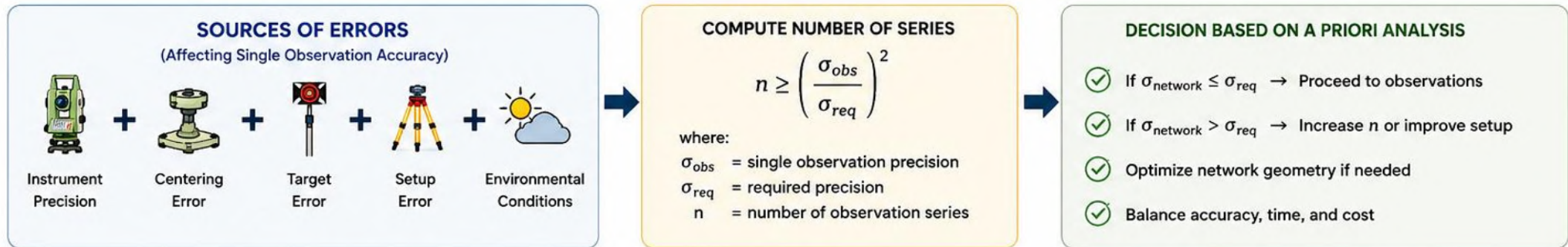
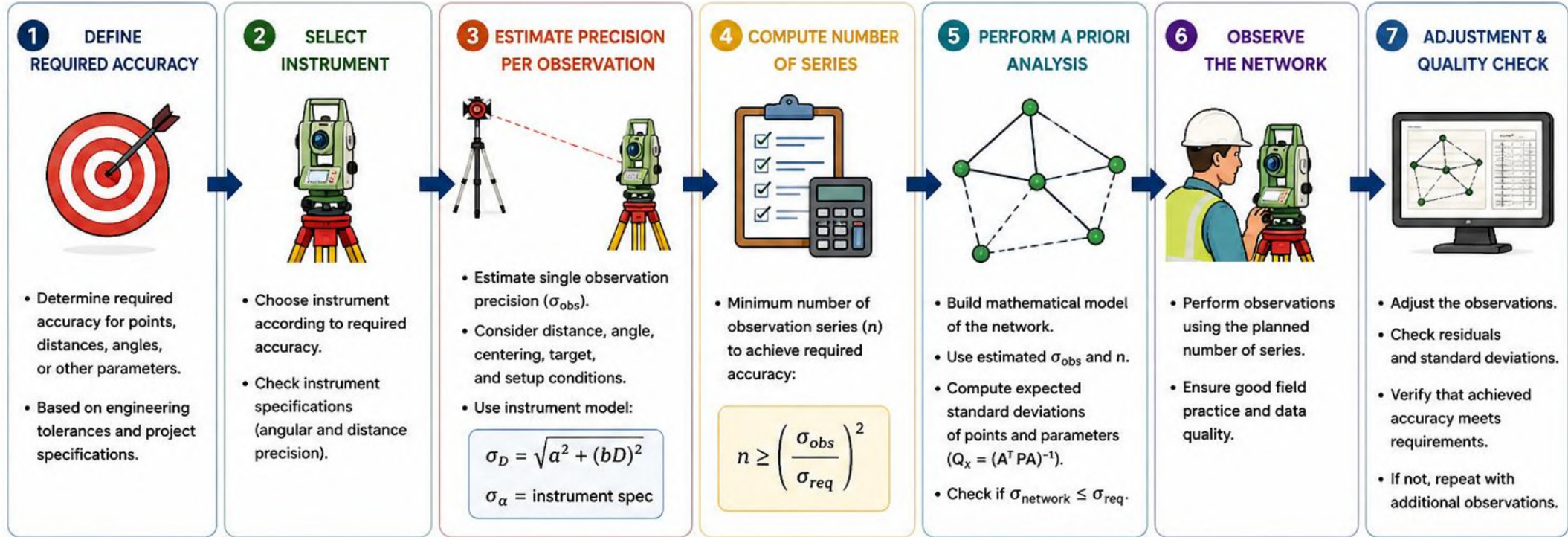
where:

- $a$  = constant term (mm)
- $b$  = ppm term
- $D$  = measured distance

Required number of series:

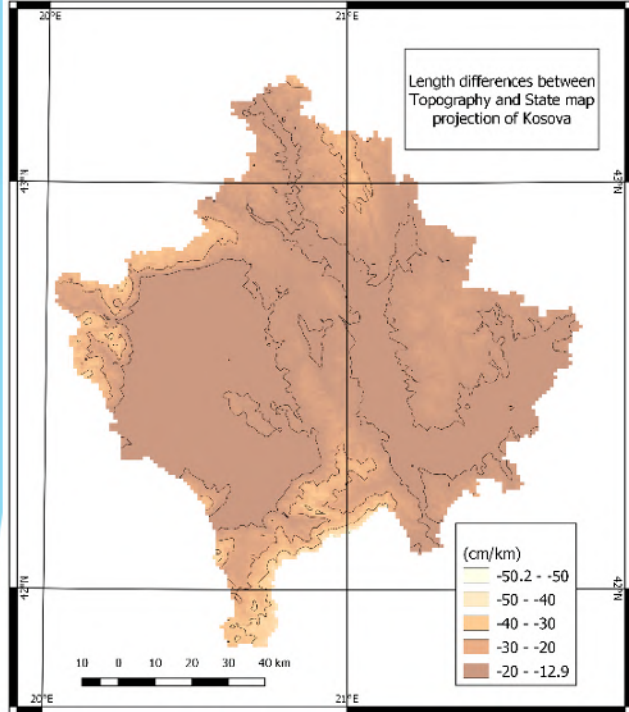
$$n \geq \left( \frac{\sigma_D}{\sigma_{required}} \right)^2$$

# OBSERVATION PLANNING – PRACTICAL FLOW



**GOAL: ACHIEVE REQUIRED ACCURACY WITH OPTIMAL EFFORT**

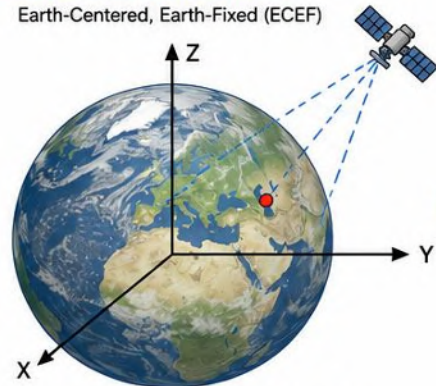
Right accuracy – Right method – Right measurement – Right result



# Ground Coordinate System

## 1. Global Reference System

Earth-Centered, Earth-Fixed (ECEF)



GNSS observations provide 3D coordinates (X, Y, Z)

## 2. National / Projected CRS

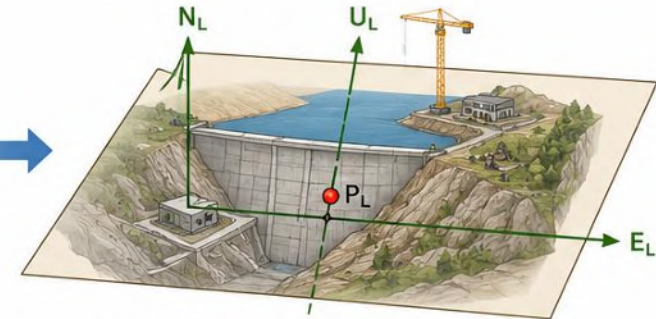
Map Projection (e.g. Gauss-Krüger)



Projection distortions (scale, angles, distances) increase with distance from central meridian.

## 3. Ground Coordinate System (Local)

Local Tangent Plane / Engineering CRS



Local origin ( $O_L$ ), orientation and scale chosen so that  $k \approx 1$  in the project area. Minimizes distortions for engineering work.

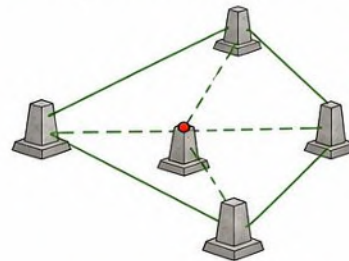
### Transformation to Local System

Translation (origin) + Rotation (azimuth) + Scale ( $k \approx 1$ )

Local Coordinates: ( $E_L, N_L, U_L$ )

## 4. Local Engineering Network

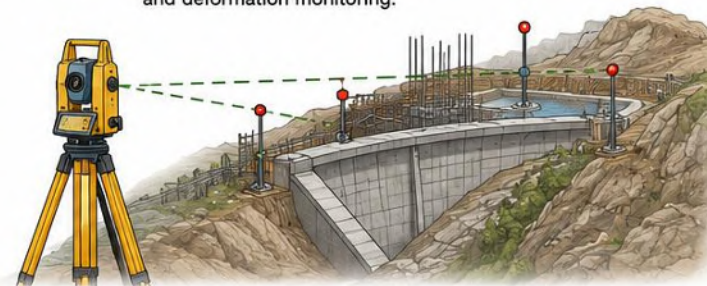
Control points established by GNSS and adjusted in the local system.



- ✓ High internal consistency
- ✓ Minimal projection distortion
- ✓ Suitable for setting-out, construction and monitoring
- ✓ Stable and reliable reference for the whole project

## 5. Engineering Applications

Setting-out, construction control and deformation monitoring.



### Benefits of GCS

- ✓ Works in true ground distances and angles
- ✓ Avoids errors caused by map projection
- ✓ Achieves required accuracy for engineering tolerances
- ✓ Ideal for large and complex structures

Distortion Range (cm/km)	ppm	Kosovaref01 (km <sup>2</sup> )	Kosovaref01 (%)
12.9-15	129-150	768	7.1%
15-20	150-200	3848	35.3%
20-25	200-250	3789	34.8%
25-30	250-300	1288	11.8%
30-40	300-400	1006	9.2%
40-50	400-500	192	1.76%
>50	>500	2	0.02%



GNSS Satellite



Control Point (Monument)



Point of Interest

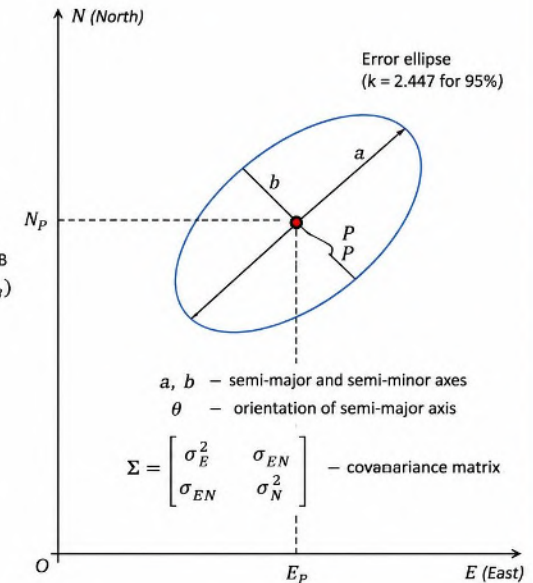
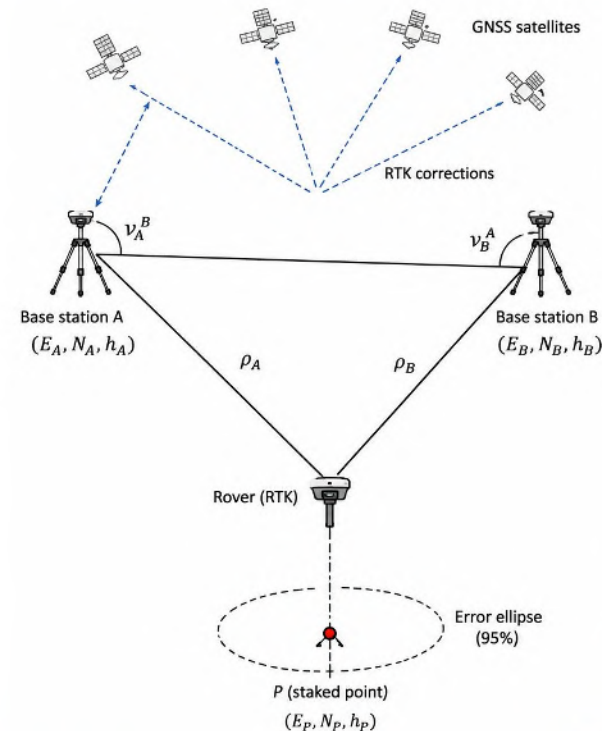
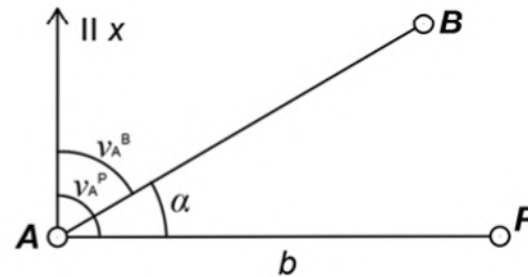
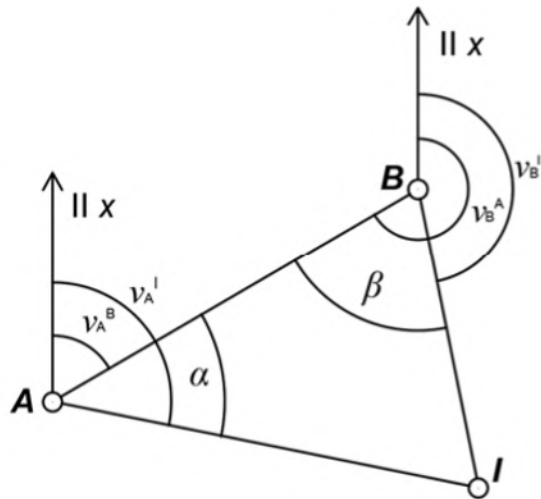
— Network Baseline

- - - Local Coordinate Axes

$N_L, E_L, U_L$  Local Axes

# STAKEOUT AND ERROR ELLIPSES

- horizontal stakeout by the method of the intersection of the sight lines,
- horizontal stakeout by the polar method, and
- horizontal stakeout by the GPS/RTK method.



Stakeout residual vector  $\Delta P = [\Delta E \quad \Delta N]^T$   
 Position error  $d_{2D} = \sqrt{\Delta E^2 + \Delta N^2}$

## Horizontal stakeout by the method of the intersection of the sight lines

To calculate the horizontal stakeout quality for the intersection method, it is necessary to start from the equation for calculating the coordinates of points using the method of the intersection:

$$y_I = y_A + \Delta y = y_A + \overline{AI} \sin v_A^I = y_A + \overline{AB} \frac{\sin \beta}{\sin(\alpha + \beta)} \sin(v_A^B + \alpha),$$

$$x_I = x_A + \Delta x = x_A + \overline{AI} \cos v_A^I = x_A + \overline{AB} \frac{\sin \beta}{\sin(\alpha + \beta)} \cos(v_A^B + \alpha),$$

or for control:

$$y_I = y_B + \Delta y = y_B + \overline{BI} \sin v_B^I = y_B + \overline{AB} \frac{\sin \alpha}{\sin(\alpha + \beta)} \sin(v_B^A - \beta),$$

$$x_I = x_B + \Delta x = x_B + \overline{BI} \cos v_B^I = x_B + \overline{AB} \frac{\sin \alpha}{\sin(\alpha + \beta)} \cos(v_B^A - \beta),$$

$$\sigma_{y_I} = \sqrt{\overline{AB}^2 \left( \frac{\cos(2\beta - v_A^B) - \cos v_A^B}{\cos(2\alpha + 2\beta) - 1} \right)^2 \sigma_\alpha^2 + \overline{AB}^2 \left( \frac{\cos v_A^B - \cos(2\alpha + v_A^B)}{\cos(2\alpha + 2\beta) - 1} \right)^2 \sigma_\beta^2},$$

$$\sigma_{x_I} = \sqrt{\overline{AB}^2 \left( \frac{\sin(2\beta - v_A^B) + \sin v_A^B}{\cos(2\alpha + 2\beta) - 1} \right)^2 \sigma_\alpha^2 + \overline{AB}^2 \left( \frac{\sin(2\alpha + v_A^B) - \sin v_A^B}{\cos(2\alpha + 2\beta) - 1} \right)^2 \sigma_\beta^2},$$

where:

$$\frac{\overline{AI}}{\overline{AB}} = \frac{\sin \beta}{\sin(180^\circ - (\alpha + \beta))} = \frac{\sin \beta}{\sin(\alpha + \beta)}$$

$$\frac{\overline{BI}}{\overline{AB}} = \frac{\sin \alpha}{\sin(180^\circ - (\alpha + \beta))} = \frac{\sin \alpha}{\sin(\alpha + \beta)}$$

$$v_A^I = v_A^B + \alpha \text{ and } v_B^I = v_B^A - \beta$$

or for control:

$$\sigma_{y_I} = \sqrt{\overline{AB}^2 \left( \frac{\cos(2\beta - v_B^A) - \cos v_B^A}{\cos(2\alpha + 2\beta) - 1} \right)^2 \sigma_\alpha^2 + \overline{AB}^2 \left( \frac{\cos v_B^A - \cos(2\alpha + v_B^A)}{\cos(2\alpha + 2\beta) - 1} \right)^2 \sigma_\beta^2},$$

$$\sigma_{x_I} = \sqrt{\overline{AB}^2 \left( \frac{\sin(2\beta - v_B^A) + \sin v_B^A}{\cos(2\alpha + 2\beta) - 1} \right)^2 \sigma_\alpha^2 + \overline{AB}^2 \left( \frac{\sin(2\alpha + v_B^A) - \sin v_B^A}{\cos(2\alpha + 2\beta) - 1} \right)^2 \sigma_\beta^2},$$

where:

$\sigma_\alpha$  and  $\sigma_\beta$  ... the standard deviations of angles  $\alpha$  and  $\beta$ .

In order to compute the error ellipse of the stakeout, the covariance must also be determined  $\sigma_{yx1}$ :

$$\sigma_{yx1} = - \frac{\overline{AB}^2 \{ [\sin(2v_A^B) + 2\sin(2\beta - 2v_A^B) - \sin(4\beta - 2v_A^B)] \sigma_\alpha^2 + [\sin(2v_A^B) - 2\sin(2\alpha + 2v_A^B) + \sin(4\alpha + 2v_A^B)] \sigma_\beta^2 \}}{\cos(4\alpha + 4\beta) - 4 \cos(2\alpha + 2\beta) + 3},$$

or for control:

$$\sigma_{yx1} = - \frac{\overline{AB}^2 \{ [\sin(2v_B^A) + 2\sin(2\beta - 2v_B^A) - \sin(4\beta - 2v_B^A)] \sigma_\alpha^2 + [\sin(2v_B^A) - 2\sin(2\alpha + 2v_B^A) + \sin(4\alpha + 2v_B^A)] \sigma_\beta^2 \}}{\cos(4\alpha + 4\beta) - 4 \cos(2\alpha + 2\beta) + 3}.$$

### Horizontal stakeout by the polar method

To calculate the horizontal stakeout quality using the polar method, it is necessary to start from the equation for calculating the coordinates of points using the polar method

$$\begin{aligned} y_P &= y_A + \Delta y = y_A + \overline{AP} \sin v_A^P = y_A + \overline{AP} \sin(v_A^B + \alpha), \\ x_P &= x_A + \Delta x = x_A + \overline{AP} \cos v_A^P = x_A + \overline{AP} \cos(v_A^B + \alpha), \end{aligned}$$

or for control:

$$\begin{aligned} y_P &= y_B + \Delta y = y_B + \overline{BP} \sin v_B^P = y_B + \overline{BP} \sin(v_B^A - \beta), \\ x_P &= x_B + \Delta x = x_B + \overline{BP} \cos v_B^P = x_B + \overline{BP} \cos(v_B^A - \beta), \end{aligned}$$

By applying the Law of propagation of variances and covariances, the precision of determining the  $y$ -coordinate of point  $P$ ,  $\sigma_{y_P}$ , and the  $x$ -coordinate of point  $P$ ,  $\sigma_{x_P}$ , is obtained:

$$\sigma_{y_P} = \sqrt{\sin^2(\alpha + \nu_A^B) \sigma_{\overline{AP}}^2 + \overline{AP}^2 \cos^2(\alpha + \nu_A^B) \sigma_\alpha^2},$$

$$\sigma_{x_P} = \sqrt{\cos^2(\alpha + \nu_A^B) \sigma_{\overline{AP}}^2 + \overline{AP}^2 \sin^2(\alpha + \nu_A^B) \sigma_\alpha^2},$$

$\sigma_{\overline{AP}}$  ... the standard deviation of distance  $\overline{AP}$ .

If the Law of propagation of variances and covariances is applied to the control equations

$$\sigma_{y_P} = \sqrt{\sin^2(\beta - \nu_B^A) \sigma_{\overline{BP}}^2 + \overline{BP}^2 \cos^2(\beta - \nu_B^A) \sigma_\beta^2},$$

$$\sigma_{x_P} = \sqrt{\cos^2(\beta - \nu_B^A) \sigma_{\overline{BP}}^2 + \overline{BP}^2 \sin^2(\beta - \nu_B^A) \sigma_\beta^2},$$

$\sigma_{\overline{BP}}$  ... the standard deviation of distance  $\overline{BP}$ ,

The error ellipses has to be calculated before stakeout and after stakeout for every point of the construction according to the following equations:

$$a = \sigma_0 \sqrt{\frac{\sigma_y^2 + \sigma_x^2 + z}{2}},$$

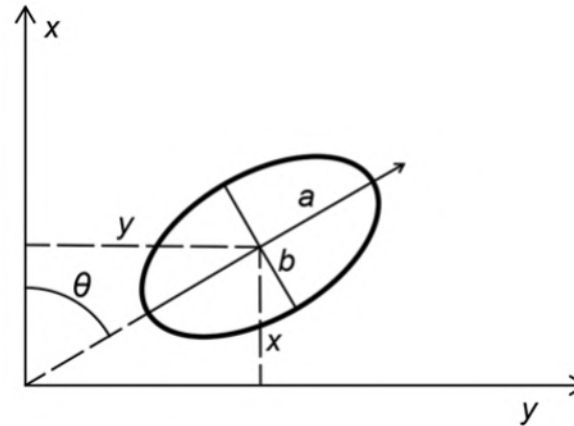
$$b = \sigma_0 \sqrt{\frac{\sigma_y^2 + \sigma_x^2 - z}{2}},$$

$$\theta = \frac{1}{2} \text{atan} \frac{2\sigma_{yx}}{\sigma_x^2 - \sigma_y^2},$$

where:

$\sigma_0$  ... the a priori reference standard deviation (typically equal to 1),

$$z = \sqrt{(\sigma_x^2 - \sigma_y^2)^2 + 4\sigma_{yx}^2}.$$



## Horizontal stakeout by GPS/RTK

For **GPS/RTK GNSS stakeout**, the mathematical model is simpler than polar/angle stakeout, because the point is positioned directly from GNSS coordinates. The error ellipse is derived from the **2D covariance matrix** of the staked point, similar to the approach used in the uploaded paper, where stakeout quality is predicted and evaluated through expected and achieved error ellipses.

### 1. Coordinate stakeout model with GPS/RTK

Let the designed point be:

$$P_D = \begin{bmatrix} E_D \\ N_D \end{bmatrix}$$

The RTK/GNSS measured or staked position is:

$$P_G = \begin{bmatrix} E_G \\ N_G \end{bmatrix}$$

The stakeout residual vector is:

$$\Delta P = \begin{bmatrix} \Delta E \\ \Delta N \end{bmatrix} = \begin{bmatrix} E_G - E_D \\ N_G - N_D \end{bmatrix}$$

The horizontal stakeout deviation is:

$$d_{2D} = \sqrt{(\Delta E)^2 + (\Delta N)^2}$$

Stakeout is acceptable if:

$$d_{2D} \leq T$$

where  $T$  is the permitted construction tolerance.

### 2. Covariance model for GPS stakeout

For RTK GNSS, the horizontal covariance matrix is:

$$\Sigma_{EN} = \begin{bmatrix} \sigma_E^2 & \sigma_{EN} \\ \sigma_{EN} & \sigma_N^2 \end{bmatrix}$$

where:

$\sigma_E$  = standard deviation in Easting

$\sigma_N$  = standard deviation in Northing

$$\sigma_{EN} = \rho \sigma_E \sigma_N$$

and  $\rho$  is the correlation coefficient between Easting and Northing.

If project coordinates also have uncertainty, then:

$$\Sigma_{\Delta} = \Sigma_{GNSS} + \Sigma_{design} + \Sigma_{control}$$

For practical RTK stakeout, often:

$$\Sigma_{\Delta} \approx \Sigma_{GNSS}$$

if design and control coordinates are treated as fixed.

### 3. Error ellipse for GPS stakeout

The semi-major and semi-minor axes are obtained from the eigenvalues of the covariance matrix:

$$\lambda_{1,2} = \frac{\sigma_E^2 + \sigma_N^2}{2} \pm \sqrt{\left(\frac{\sigma_E^2 - \sigma_N^2}{2}\right)^2 + \sigma_{EN}^2}$$

Then:

$$a = k\sqrt{\lambda_1}$$

$$b = k\sqrt{\lambda_2}$$

where:

$a$  = semi-major axis

$b$  = semi-minor axis

$k$  = confidence factor

Typical values:

$k = 1.00$  for standard ellipse

$k=2.447$  \quad \text{for 95% confidence ellipse in 2D}

### 4. Orientation of the error ellipse

The orientation angle of the ellipse is:

$$\theta = \frac{1}{2} \tan^{-1} \left( \frac{2\sigma_{EN}}{\sigma_E^2 - \sigma_N^2} \right)$$

This angle defines the direction of the semi-major axis relative to the Easting axis.

### 5. Practical GPS/RTK stakeout quality model

For each stakeout point:

$$P_i = (E_i, N_i)$$

compute:

$$d_i = \sqrt{(E_{G_i} - E_{D_i})^2 + (N_{G_i} - N_{D_i})^2}$$

and:

$$\Sigma_i = \begin{bmatrix} \sigma_{E_i}^2 & \sigma_{EN_i} \\ \sigma_{EN_i} & \sigma_{N_i}^2 \end{bmatrix}$$

Then calculate:

$$a_i, b_i, \theta_i$$

The point is acceptable if:

$$d_i \leq T$$

and preferably also:

$$a_{95,i} \leq T$$

# VERTICAL STAKEOUT ACCURACY MODEL

## 1. Leveling instrument model

Designed elevation:

$$H_D$$

Measured elevation:

$$H_L$$

Vertical stakeout residual:

$$\Delta H_L = H_L - H_D$$

Distance-dependent leveling accuracy:

$$\sigma_{H_L} = \sigma_{1km} \sqrt{L}$$

where  $L$  is leveling distance in km.

95% vertical confidence interval:

$$CI_{95,L} = \pm 1.96 \sigma_{H_L}$$

Acceptance condition:

$$|\Delta H_L| \leq T_V$$

This is the most precise model for vertical construction stakeout.



## 2. Total station model

Designed elevation:

$$H_D$$

Elevation from total station:

$$H_{TS} = H_A + h_i + s \cos z - h_p$$

where:

$H_A =$  known station elevation

$h_i =$  instrument height

$s =$  slope distance

$z =$  zenith angle

$h_p =$  prism height

Vertical residual:

$$\Delta H_{TS} = H_{TS} - H_D$$

Error propagation:

$$\sigma_{H_{TS}}^2 = \sigma_{H_A}^2 + \sigma_{h_i}^2 + \cos^2 z \sigma_s^2 + s^2 \sin^2 z \sigma_z^2 + \sigma_{h_p}^2$$

95% confidence interval:

$$CI_{95,TS} = \pm 1.96 \sigma_{H_{TS}}$$

Acceptance condition:

$$|\Delta H_{TS}| \leq T_V$$

## 3. GPS / RTK GNSS model

Designed elevation:

$$H_D$$

GNSS ellipsoidal height:

$$h_{GNSS}$$

Geoid undulation:

$$N$$

Orthometric height:

$$H_{GNSS} = h_{GNSS} - N$$

Vertical residual:

$$\Delta H_{GNSS} = H_{GNSS} - H_D$$

Variance model:

$$\sigma_{H_{GNSS}}^2 = \sigma_{h_{GNSS}}^2 + \sigma_N^2$$

If antenna height is included:

$$\sigma_{H_{GNSS}}^2 = \sigma_{h_{GNSS}}^2 + \sigma_N^2 + \sigma_{h_a}^2$$

95% confidence interval:

$$CI_{95,GNSS} = \pm 1.96 \sigma_{H_{GNSS}}$$

Acceptance condition:

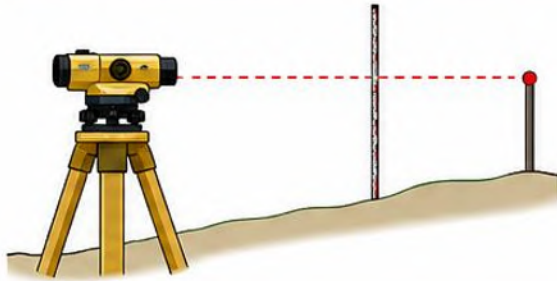
$$|\Delta H_{GNSS}| \leq T_V$$

For RTK, vertical accuracy is usually weaker than horizontal accuracy, so GNSS is less suitable than leveling for strict vertical construction tolerances.

# Which Method Should Be Used?

## LEVELING

Highest Vertical Accuracy



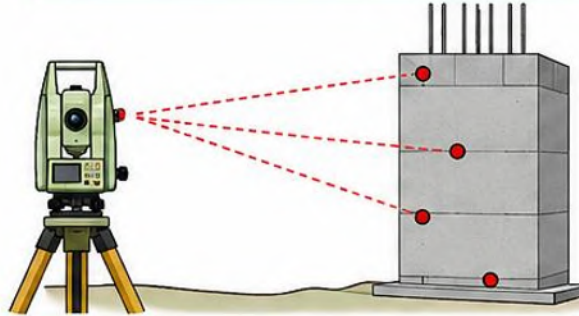
- Precise height determination
- Long range capability
- Not affected by short-term atmospheric conditions
- Slower field work



Best choice when vertical accuracy is critical

## TOTAL STATION

High Local Precision



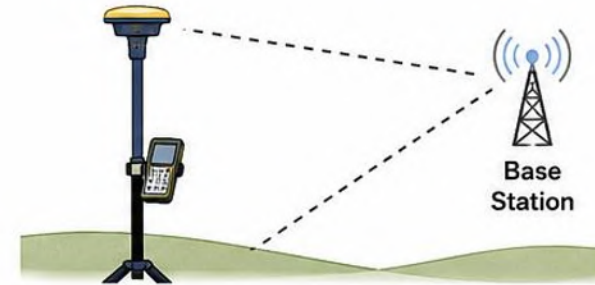
- High angular and distance accuracy
- Ideal for local control and staking
- Suitable for deformation monitoring
- Moderate field time



Best choice for most construction and monitoring tasks

## RTK GNSS

Fast Field Operations



- Rapid point determination
- Efficient for large areas
- Lower precision than total station and leveling
- Dependent on satellite availability and corrections



Best choice when speed and efficiency are priorities



**General Rule:** Use the method that satisfies the required accuracy with the least field time and resources.

# GEODETIC DEFORMATION ANALYSES

## Objective

Separate:

*Observed Changes = True Deformation + Random Errors*

Main problem:

Two epochs:

$Epoch_1 \rightarrow Epoch_2$

Determine:

- Which points are stable?
- Which points moved?
- How significant is movement?

## General Adjustment Model

Observation equations:

$$Ax + v = l$$

Adjustment:

$$\hat{x} = (A^T P A)^{-1} A^T P l$$

Deformation vector:

$$d = x_2 - x_1$$

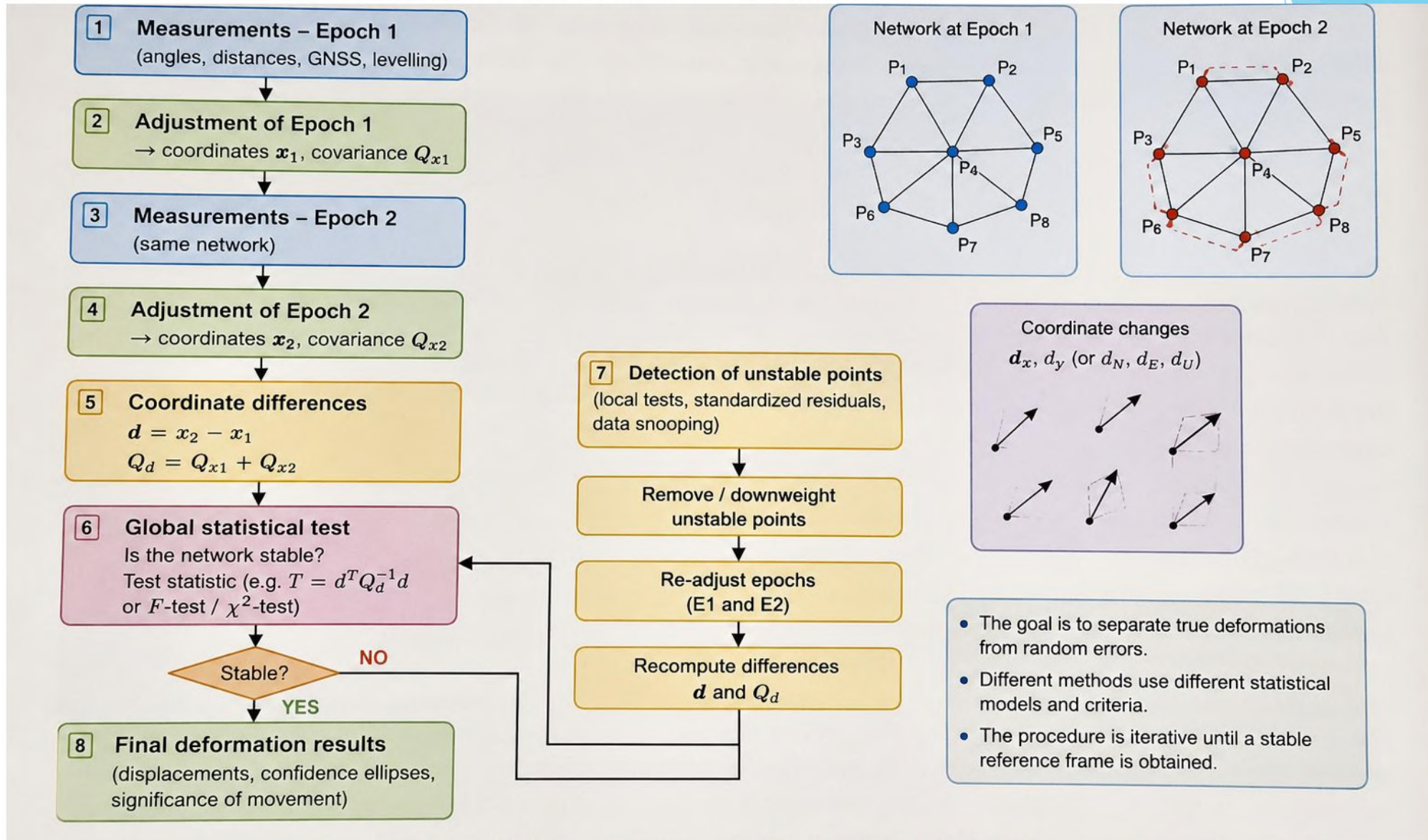
Covariance:

$$Q_d = Q_{x_1} + Q_{x_2}$$

“testing whether  $H_0: d=0$ ”

*Testing whether displacement vector equals zero.*

# Typical Deformation Analysis Procedure



*This logic is common to almost all methods.*

## Pelzer Method (Hannover School)

### Step 1

Assume reference points stable

### Step 2

Compute deformation vector

$$d = x_2 - x_1$$

Test statistic:

$$T = \frac{d^T Q_d^{-1} d}{h\sigma_0^2}$$

Decision:

If:

$$T > F_\alpha$$

↓

Network not stable

### Step 3

Localize unstable points

Remove suspect point

Recompute: A,B,C,D,E

↓

remove B

↓

A,C,D,E

↓

test again

*Repeat until Global test accepted!*

*Iteratively eliminate the point with the largest contribution to instability until the global test is accepted.*

### Practical Use

✓ Dams

✓ Bridges

✓ Buildings

✓ Monitoring with stable monuments

## Caspary Method

Core principle:

Direct testing of coordinate changes.

Statistic:

$$w = d^T Q_d^{-1} d$$

Decision:

$$w > \chi^2$$

↓

movement detected

Procedure:

Compute coordinate changes

↓

Test significance

↓

Point stable?

YES → keep

NO → deforming point

*Point displacement is accepted only if the displacement vector is statistically significant compared with its covariance.*

### Practical Use

- ✓ Engineering monitoring
- ✓ Small-medium networks
- ✓ Construction control

## Delft Method

Core idea:

### Congruency between epochs

Null hypothesis:

$$H_0: d = 0$$

Compare:

Constrained solution

vs

Free solution

### Adjust Both Epochs

Constrained solution

$$v_c^T P v_c$$

(Adjustment with constraints)

↓

Free solution

$$v_f^T P v_f$$

(Adjustment without constraints)

### Compare Both Solutions

Statistic:

$$F = \frac{(v_c P v_c - v_f P v_f)/q}{(v_f P v_f)/f}$$

Decision:

$$F > F_{crit}$$

↓

epochs inconsistent

↓

Deformation exists

*Congruency test compares constrained and free network solutions between epochs*

### Practical Use

- ✓ High precision monitoring
- ✓ Research networks
- ✓ Scientific deformation studies
- ✓ Crustal movement studies

## Karlsruhe Method

Problem:

Reference points may also move.

Solution:

Free network adjustment.

Transformation:

$$x_c = x_f - Sk$$

Concept:

Remove datum dependency.

Procedure:

Free adjustment



S transformation



Compute deformation



Reference independent result

*Recommended when reference points cannot be assumed stable.*

### Practical Use

- ✓ Landslides
- ✓ Mining subsidence
- ✓ Large unstable areas
- ✓ Tectonic monitoring

## YU Method

### Core Philosophy

Stable coordinate system = stable deformation results

Unlike Pelzer / Delft / Karlsruhe:

- Uses **conventional datum**
- No optimal datum definition
- No S-transformations
- Requires stable coordinate system definition

Number of possible sides:

$$r = \frac{n(n-1)}{2}$$

### Test Length Differences

Hypotheses:

$$H_0: \Delta S_i = 0$$

$$H_A: \Delta S_i \neq 0$$

Statistical test:

$$t_i = \frac{\Delta S_i}{\sigma_{\Delta S_i}}$$

Decision:

If:

$$t_i < t_{\alpha/2}$$

↓

Length considered stable

Otherwise:

↓

Reject side

### Practical Use:

- ✓ Small monitoring networks
- ✓ Conventional engineering workflows
- ✓ Existing legacy monitoring systems
- ✓ Faster calculations

### Test Azimuth Differences

Hypotheses:

$$H_0: \Delta \phi_i = 0$$

$$H_A: \Delta \phi_i \neq 0$$

Statistic:

$$t_i = \frac{\Delta \phi_i}{\sigma_{\Delta \phi_i}}$$

Decision:

If:

$$t_i < t_{\alpha/2}$$

↓

Point group considered stable

Otherwise:

↓

Reject candidate group.

## Comparison of Practical Applications of Deformation Analysis Methods

Method	Recommended When	Not Recommended When	Typical Applications	Main Strength
Pelzer (Hannover School)	Stable reference points exist and can be reliably identified	Reference points may move or stability is uncertain	Dams, bridges, buildings, classical engineering monitoring	Robust iterative stability testing
Caspary Method	Simple and efficient deformation testing is required	Large unstable networks or uncertain datum conditions	Construction monitoring, industrial monitoring, small-medium networks	Simple implementation with direct significance testing
Delft Method	High statistical rigor and congruency analysis are required	Fast operational projects with limited computational resources	Scientific monitoring, crustal deformation, research networks	Strong statistical framework
Karlsruhe Method	Reference point stability cannot be guaranteed	Small simple projects with clearly stable control points	Landslides, mining subsidence, tectonic monitoring	Datum-independent deformation estimation
Former Yugoslav School	Conventional datum and stable coordinate systems are available	Stable datum cannot be confirmed	Classical monitoring networks, legacy engineering workflows	Faster computations and simpler implementation

**No universal best method exists.**

**Method selection depends primarily on:**

- Reference point stability
- Network geometry
- Required statistical rigor
- Type of engineering object

# Multi-Temporal InSAR Method (PSInSAR / QPSInSAR)

## Core Philosophy

Deformation is estimated from phase differences between repeated SAR acquisitions

Unlike classical geodetic methods:

- No physical network required
- Millions of monitoring points possible
- Spatially continuous monitoring
- Large-area deformation mapping possible

## Step 1 - Acquire Multi-Temporal SAR Images

Repeated SAR acquisitions:

$t_1 \rightarrow t_2 \rightarrow t_3 \rightarrow t_4 \rightarrow \dots \rightarrow t_n$

Ascending + Descending orbits frequently used.

## Step 2 - Generate Interferograms

Interferometric phase:

$$\Delta\phi = \phi_2 - \phi_1$$

Generate multiple interferograms.

STAR graphs commonly define interferometric connectivity.

## Step 3 - Differential Phase Model

Observed phase:

$$\Delta\phi = \Delta\phi_{disp} + \Delta\phi_{topo} + \Delta\phi_{atmo} + \Delta\phi_{noise}$$

where:

- deformation component
- topographic component
- atmospheric component
- noise component

## Step 4 - Remove Unwanted Components

Corrections:

- ✓ orbital corrections
- ✓ topographic corrections
- ✓ earth flattening
- ✓ atmospheric correction (APS)

Result:

$$\Delta\phi \rightarrow \Delta\phi_{disp}$$

## Step 5 - Compute LOS Displacement

LOS displacement:

$$d_{LOS} = \frac{\lambda}{4\pi} \Delta\phi_{disp}$$

where:

- $\lambda$  = wavelength
- LOS = line of sight displacement

## Step 6 - Select Stable Scatterers

### Persistent Scatterers (PS)

- stable phase behavior
- buildings
- infrastructure
- rocks

### Distributed Scatterers (DS)

- spatially homogeneous areas
- vegetation
- natural surfaces

## Step 7 - Time Series Analysis

Estimate:

$$v = \frac{d}{dt}$$

Compute:

- displacement velocity
- nonlinear motion
- seasonal signals
- long-term trends

## Step 8 - Interpretation and Validation Objective

Validate deformation results and transform them into engineering information.

### Accuracy Assessment

Compare InSAR results with independent measurements:

- GNSS observations
- Leveling measurements
- Total station measurements

### Validation Model

Difference between methods:

$$\Delta d = d_{InSAR} - d_{Reference}$$

Compute validation statistics:

$$RMSE = \sqrt{\frac{\sum (d_{InSAR} - d_{Reference})^2}{n}}$$

where:

- $d_{InSAR}$  = InSAR displacement
- $d_{Reference}$  = reference displacement
- $n$  = number of validation points

# PRACTICAL WORKFLOW

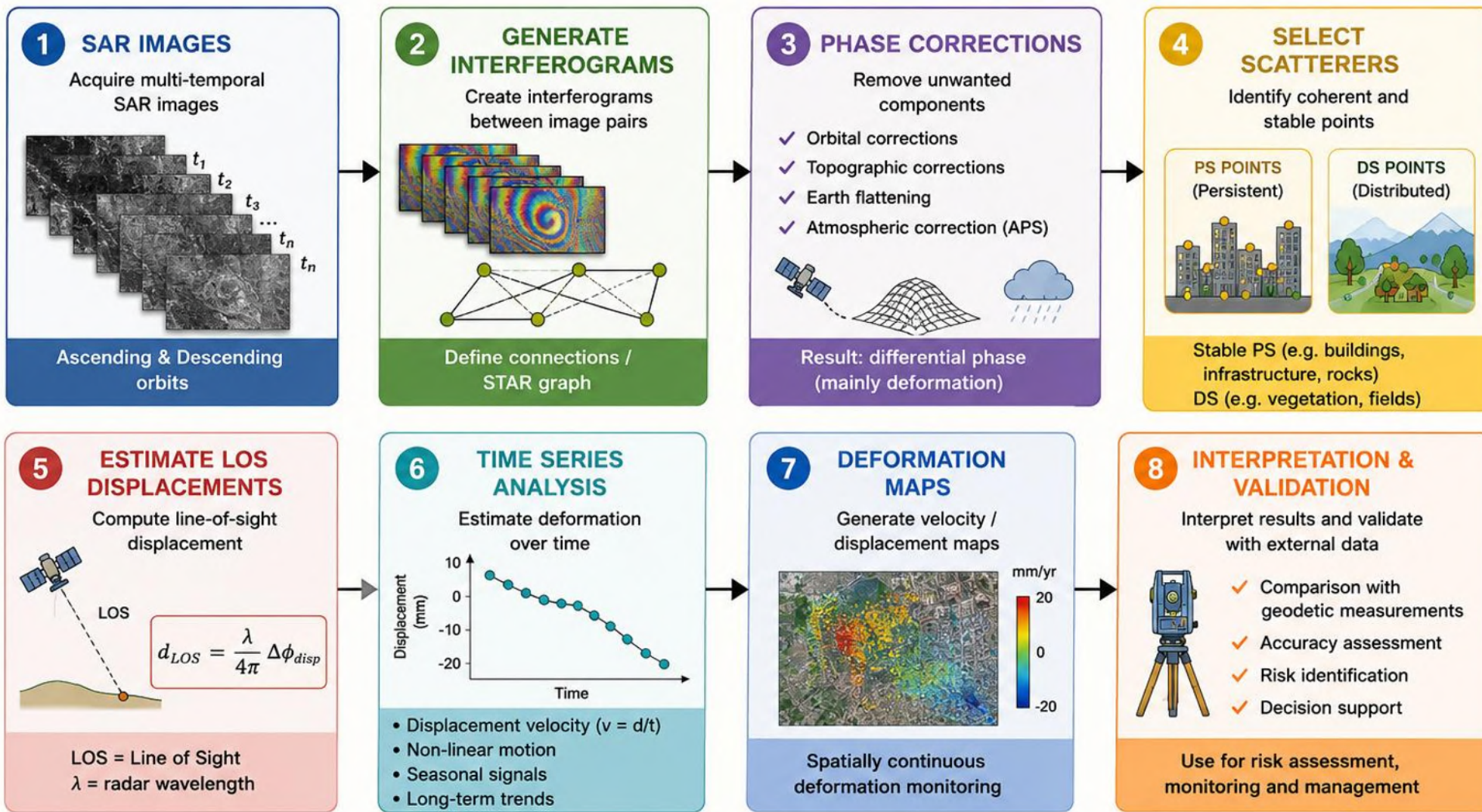
## InSAR Deformation Monitoring (PSInSAR / QPSInSAR)

### Suitable for:

- ✓ Landslides
- ✓ Mining subsidence
- ✓ Urban subsidence
- ✓ Regional tectonics
- ✓ Dam monitoring
- ✓ Large infrastructure monitoring

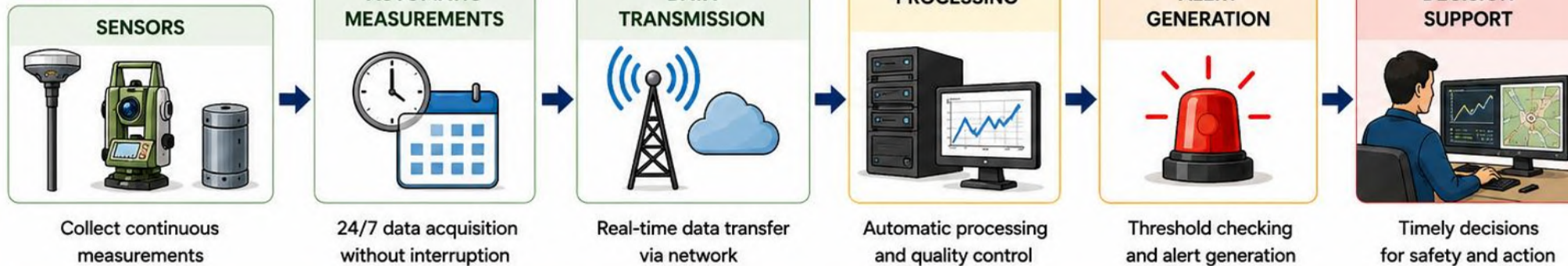
### Less Suitable for:

- ✗ Dense vegetation
- ✗ Rapid decorrelation
- ✗ Need for real-time monitoring
- ✗ North-South displacement sensitivity limitations



# ONLINE GEODETIC MONITORING SYSTEMS

## CORE IDEA



## GOAL

- ✓ Detect movement immediately
- ✓ Reduce risk
- ✓ Increase safety
- ✓ Continuous observation

## TYPICAL OBJECTS



Dams



Bridges



Landslides



Tunnels

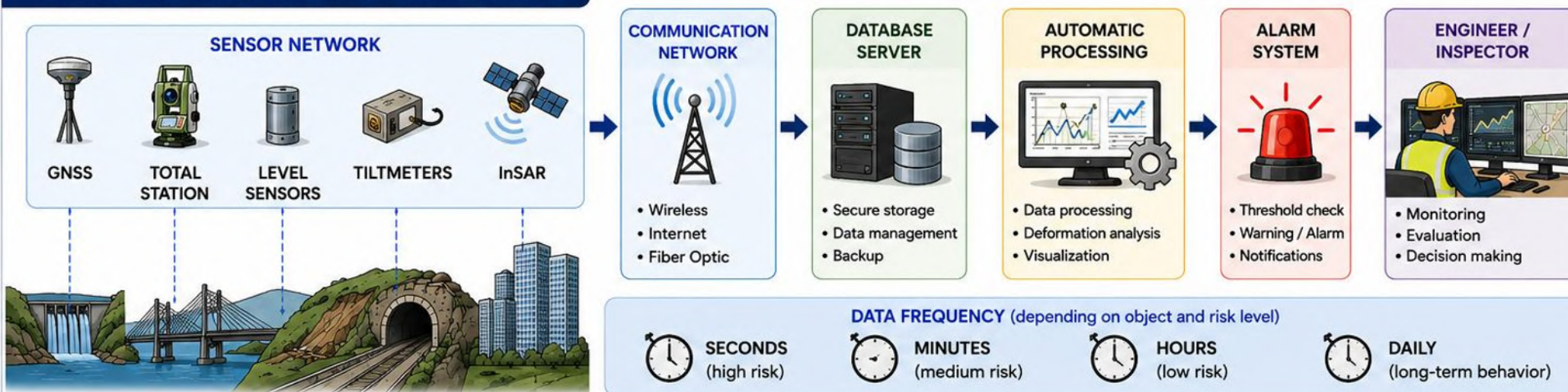


High-rise Buildings



Mining Areas

## TYPICAL MONITORING ARCHITECTURE

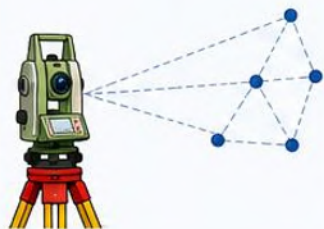


# MATHEMATICAL MONITORING MODEL

## OBSERVATION VECTOR

Observation vector  
at time  $t$

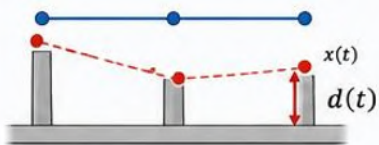
$$l(t)$$



## DEFORMATION

Deformation at time  $t$

$$d(t) = x(t) - x_0$$

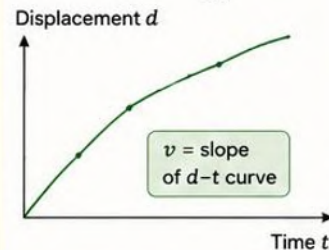


—  $x_0$  Initial position  
- - -  $x(t)$  Position at time  $t$

## VELOCITY

Velocity

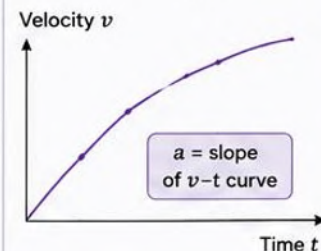
$$v = \frac{dx}{dt}$$



## ACCELERATION

Acceleration

$$a = \frac{dv}{dt}$$



## ALARM CONDITION

Alarm is triggered when:

$$|d| > d_{\text{critical}}$$

or

$$|v| > v_{\text{critical}}$$



## MONITORING STRATEGIES

OBJECT	RECOMMENDED SENSORS	FREQUENCY	TYPICAL RISK
BRIDGES	GNSS + TOTAL STATION	SECONDS - MINUTES	STRUCTURAL MOVEMENT
DAMS	GNSS + TOTAL STATION + LEVELING	MINUTES - HOURS	STABILITY
LANDSLIDES	GNSS +	MINUTES - DAYS	SLOPE FAILURE
BUILDINGS	TOTAL STATION + LEVELING	MINUTES - HOURS	SETTLEMENT
TUNNELS	TOTAL STATION + TILTMETERS	SECONDS - MINUTES	DISPLACEMENT

## DECISION RULE



## INTERVENTION



- ✓ Immediate notification
- ✓ Detailed analysis
- ✓ Report generation
- ✓ Action and mitigation measures

## KEY BENEFITS OF ONLINE GEODETIC MONITORING



Real-time detection of movement



Improved safety and risk reduction



Continuous data for better decisions



Cost and downtime reduction



Documentation and traceability

# CATEGORIZATION OF STRUCTURES AND PROJECT PHASES

EVERY PROJECT MUST PASS THROUGH ALL PHASES: DESIGN – REVISION – IMPLEMENTATION – SUPERVISION

A

## CATEGORY A

### HIGH CONSEQUENCE STRUCTURES

Structures of high importance and complexity, where failure may result in significant loss of life, economic or environmental impact.



Large Bridges



Dams and Hydraulic Structures



High-Rise and Complex Buildings



Tunnels and Underground Works



Industrial Plants and Facilities

## CATEGORY B

### STANDARD RISK STRUCTURES

Structures of moderate importance and standard complexity, with limited consequences in case of failure.

B



Residential Buildings  
(up to 3 stories)



Light Industrial Structures



Roads  
(not highways)




Neighborhood Leveling (Plaza)




Agricultural Structures

**1 DESIGN**



- Detailed site investigation
- Geodetic control network design
- Structural design
- Advanced analysis and modeling
- Technical specifications

**2 REVISION**




- Independent design revision
- Code and standard compliance
- Geodetic accuracy assessment
- Risk analysis
- Approval / comments

**3 IMPLEMENTATION**




- Precision setting out
- Construction with strict quality control
- Continuous geodetic monitoring
- As-built documentation

**4 SUPERVISION**




- Independent geodetic supervision
- Continuous monitoring and analysis
- Deviation and risk assessment
- Final acceptance and performance verification

**1 DESIGN**




- Site investigation and analysis
- Geodetic plan
- Structural design
- Drawings & calculations
- Technical specifications

**2 REVISION**




- Design check
- Compliance with codes and standards
- Geodetic network verification
- Approval / comments

**3 IMPLEMENTATION**



- Setting out
- Construction execution
- Geodetic measurements during construction
- As-built documentation

**4 SUPERVISION**



- Geodetic supervision
- Quality control
- Deviation analysis
- Reports and records
- Final acceptance

## KEY PRINCIPLES FOR ALL PROJECTS



### SAFETY FIRST

Protecting people, property and the environment.



### COMPLIANCE

Meet all legal requirements and technical standards.



### QUALITY

Ensure quality in every phase with proper control and documentation.



### ROLES & RESPONSIBILITIES

Clear definition of roles for designer, reviewer, contractor and supervisor.



### DOCUMENTATION

All phases must be documented, archived and traceable.



### CONTINUOUS IMPROVEMENT

Learn from experience and improve processes for future projects.



Bridges



Dams



Buildings



Tunnels



Industrial Plants



Residential



Industrial



Roads



Neighborhood Leveling



Agricultural

## CONCLUSIONS

1. Successful engineering surveying requires integration of network design, measurement planning, stakeout quality control and monitoring strategies.
2. A priori accuracy analysis is essential to prove that geodetic networks can satisfy engineering tolerances before field measurements begin.
3. Local geodetic monitoring networks combined with rigorous adjustment procedures enable reliable detection of structural deformations.
4. Deformation analysis results strongly depend on reference point stability, network geometry and the selected mathematical model.
5. No universal deformation analysis method exists; method selection depends on object type, stability conditions and monitoring objectives.
6. Automated monitoring systems and satellite-based monitoring techniques significantly improve monitoring efficiency and spatial coverage.
7. Early detection and continuous monitoring are fundamental for infrastructure safety, risk reduction and informed engineering decisions.

**Pyetje & Diskutime !!!**

# Faleminderit për vëmendjen!

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